associate via a complex network of $\mathrm{N}-\mathrm{H} \cdots \mathrm{O}$ hydrogen bonds and dipolar attractions, utilizing most of the available amide and carbonyl functional groups.

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# Structure of Demethylsterigmatocystin 

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#### Abstract

C}_{17} \mathrm{H}_{10} \mathrm{O}_{6}, M_{r}=310 \cdot 3\), monoclinic, $C 2, a=$ 16.359 (3), $b=7.099$ (1), $c=12.150$ (1) $\AA, \beta=$ $107.71(1)^{\circ}, D_{x}=1.53 \mathrm{Mg} \mathrm{m}^{-3}$ for $Z=4$. The structure was refined by the block-diagonal leastsquares method to $R=0.068$ for 962 non-zero reflections. The xanthone skeleton is slightly twisted to take a propeller-like form.


Introduction. The title compound was isolated from Aspergillus versicolor (Vuillemin) Tiraboschi, and was shown to be a demethyl derivative of sterigmatocystin (Elsworthy, Holker, McKeown, Robinson \& Mulheirn, 1970). The present X-ray analysis was undertaken to reveal the conformation of the dihydrofuro[2,3-b]furan moiety which is a common structural unit in toxic metabolites of the genus $A$ spergillus.

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Pale yellow needle-shaped crystals elongated along the $b$ axis were obtained from acetone solution. The systematic absences uniquely characterized the space group as $C 2$, since the compound has optical activity. The unit-cell constants were obtained by least-squares refinement of the setting angles measured on a fourcircle diffractometer. The intensities were measured on a Rigaku computer-controlled four-circle diffractometer using Ni -filtered $\mathrm{Cu} K a$ radiation from a crystal cut to approximate dimensions of $0.1 \times 0.3 \times 0.1 \mathrm{~mm}$. The $\theta-2 \theta$ scan technique was employed with a scan speed of $4^{\circ} \min ^{-1}$ in $2 \theta$. The scan range for $\theta$ was calculated as $1.0^{\circ}+0.15^{\circ} \tan \theta$. The backgrounds were counted for 10 s at both sides of the scan range. The intensities of 1081 reflections were measured within the range $2 \theta \leq 120^{\circ}$; 962 of these were nonzero, and corrected for Lorentz and polarization factors only. The structure was solved by interpretation of the Patterson function, and refined by block-diagonal least-squares calculations (Ashida, 1973) with anisotropic temperature factors for heavy atoms and fixed isotropic temperature factors ( $4 \cdot 0 \AA^{2}$ ) © 1979 International Union of Crystallography
for H atoms, where unit weight was applied for each reflection. The final $R$ value was 0.068 for all non-zero reflections. The atomic scattering factors were taken from International Tables for X-ray Crystallography (1962). The final atomic coordinates are given in Table 1.*

Discussion. The molecular structure is shown in Fig. 1, together with the atomic numbering used in this paper; the configurations around $\mathrm{C}(14)$ and $\mathrm{C}(17)$ were assumed to be the same as those in related molecules established by the X-ray method (Fukuyama, Hamada, Tsukihara \& Katsube, 1978; Bear, Waters \& Waters, 1970). The bond lengths and angles for non-hydrogen atoms are shown in Table 2, and the equations of leastsquares planes and the deviations of atoms from each plane are in Table 3.

> * Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34174 ( 6 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

Table 1. Final atomic coordinates ( $\times 10^{4}$ for nonhydrogen atoms and $\times 10^{3}$ for hydrogen atoms)

|  |  | $x$ |  | $y$ | $z$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| C(1) |  | 1274 (5) |  | 2641 (18) | 1115 (7) |
| C(2) |  | 1047 (5) |  | 2723 (16) | 2105 (7) |
| C(3) |  | 1662 (5) |  | 2610 (16) | 3219 (6) |
| C(4) |  | 1418 (5) |  | 2641 (18) | 4256 (7) |
| C(5) |  | 2114 (5) |  | 2491 (15) | 5342 (6) |
| C(6) |  | 1974 (5) |  | 2544 (15) | 6432 (6) |
| $\mathrm{C}(7)$ |  | 2638 (6) |  | 2507 (16) | 7427 (7) |
| C(8) |  | 3473 (6) |  | 2360 (15) | 7386 (7) |
| C(9) |  | 3658 (6) |  | 2314 (16) | 6337 (7) |
| $\mathrm{C}(10)$ |  | 2972 (5) |  | 2400 (16) | 5349 (6) |
| $\mathrm{C}(11)$ |  | 2532 (5) |  | 2351 (15) | 3286 (6) |
| C (12) |  | 2775 (5) |  | 2155 (15) | 2305 (7) |
| C(13) |  | 2136 (6) |  | 2286 (15) | 1259 (6) |
| C(14) |  | 3352 (7) |  | 1452 (17) | 792 (8) |
| C(15) |  | 4226 (7) |  | 4030 (17) | 1160 (9) |
| C(16) |  | 4151 (6) |  | 3688 (16) | 2182 (8) |
| C(17) |  | 3639 (6) |  | 1860 (16) | 2121 (7) |
| $\mathrm{O}(1)$ |  | 212 (4) |  | 3034 (12) | 2006 (5) |
| $\mathrm{O}(2)$ |  | 658 (4) |  | 2824 (13) | 4252 (5) |
| $\mathrm{O}(3)$ |  | 1158 (4) |  | 2710 (13) | 6496 (5) |
| $\mathrm{O}(4)$ |  | 3168 (3) |  | 2283 (10) | 4319 (4) |
| $\mathrm{O}(5)$ |  | 2453 (4) |  | 2002 (12) | 347 (4) |
| O (6) |  | 3841 (4) |  | 2733 (16) | 321 (5) |
|  | Bonded to |  | $x$ | $y$ | $z$ |
| H(1) | C (1) |  | 88 (6) | 175 (18) | 39 (8) |
| H(2) | $\mathrm{O}(1)$ |  | 15 (6) | 293 (19) | 246 (8) |
| H(3) | $\mathrm{O}(3)$ |  | 94 (6) | ) 287 (20) | 591 (8) |
| H(4) | C(7) |  | 259 (6) | ) 233 (19) | 807 (8) |
| H(5) | C(8) |  | 390 (6) | 224(19) | 799 (8) |
| H(6) | C(9) |  | 427 (6) | 213(19) | 633 (8) |
| H(7) | C (14) |  | 341 (7) | ) 15 (19) | 56 (9) |
| H(8) | C(15) |  | 457 (7) | 509(19) | 103 (9) |
| H(9) | C(16) |  | 433 (6) | 470(18) | 277 (9) |
| H(10) | C (17) |  | 400 (7) | ) 44 (19) | 263 (9) |

There are two intramolecular hydrogen bonds: $\mathrm{O}(1)-\mathrm{H}(2) \cdots \mathrm{O}(2)$ and $\mathrm{O}(3)-\mathrm{H}(3) \cdots \mathrm{O}(2)$. The distances $\mathrm{O}(2) \cdots \mathrm{H}(2)$ and $\mathrm{O}(2) \cdots \mathrm{H}(3)$ are 2.08 and $1.93 \AA$, respectively, and the angles $\mathrm{O}(1)-\mathrm{H}(2) \cdots \mathrm{O}(2)$ and $\mathrm{O}(3)-\mathrm{H}(3) \cdots \mathrm{O}(2)$ are 148 and $161^{\circ}$. Comparison of the bond angles $\mathrm{C}(3)-\mathrm{C}(2)-\mathrm{O}(1)$ and $\mathrm{C}(5)-\mathrm{C}(6)-$ $\mathrm{O}(3)$ with those of related compounds has shown that the angle involving the hydroxyl group as a side chain is larger by a few degrees than that involving the methoxy group. The same effect has been observed in other compounds, and interpreted by Coppens \& Schmidt (1965). The other bond lengths and angles in the xanthone skeleton seem to be the same as those


Fig. J. Molecular structure of demethylsterigmatocystin plotted by a local version of PLUTO (Motherwell, 1976).

Table 2. Bond lengths ( $\AA$ ) and angles ( ${ }^{\circ}$ ) with estimated standard deviations in parentheses

| $\mathrm{C}(1)-\mathrm{C}(2) \quad 1$. | 1.365 (17) | $\mathrm{C}(1)-\mathrm{C}(13) \quad 1$ | $1 \cdot 390$ (17) |
| :---: | :---: | :---: | :---: |
| $\mathrm{C}(2)-\mathrm{C}(3) \quad 1$. | 1.421 (16) | $\mathrm{C}(2)-\mathrm{O}(1) \quad 1$ | $1 \cdot 352$ (14) |
| $\mathrm{C}(3)-\mathrm{C}(4) \quad 1$. | 1.433 (17) | $\mathrm{C}(3)-\mathrm{C}(11) \quad 1$. | 1.414 (15) |
| $\mathrm{C}(4)-\mathrm{C}(5) \quad 1$. | 1.461 (16) | $\mathrm{C}(4)-\mathrm{O}(2) \quad 1$ | 1.248 (15) |
| $\mathrm{C}(5)-\mathrm{C}(6) \quad 1$. | 1.413 (15) | $\mathrm{C}(5)-\mathrm{C}(10) \quad 1$ | 1.402 (15) |
| $\mathrm{C}(6)-\mathrm{C}(7) \quad 1$. | 1.358 (16) | $\mathrm{C}(6)-\mathrm{O}(3) \quad 1$ | 1.365 (14) |
| $\mathrm{C}(7)-\mathrm{C}(8) \quad 1.38$ | 1.386 (16) | $\mathrm{C}(8)-\mathrm{C}(9)$. 1 | 1.397 (16) |
| $\mathrm{C}(9)-\mathrm{C}(10) \quad 1$. | 1.373 (16) | $\mathrm{C}(10)-\mathrm{O}(4) \quad 1$ | $1 \cdot 386$ (13) |
| $\mathrm{C}(11)-\mathrm{C}(12) \quad 1$. | 1.374 (15) | $\mathrm{C}(11)-\mathrm{O}(4) \quad 1$ | 1.366 (13) |
| $\mathrm{C}(12)-\mathrm{C}(13) \quad 1$. | 1.382 (15) | $\mathrm{C}(12)-\mathrm{C}(17) \quad 1$ | 1.511 (16) |
| $\mathrm{C}(13)-\mathrm{O} 5) \quad 1$. | 1.373 (14) | $\mathrm{C}(14)-\mathrm{C}(17) \quad 1$ | 1.565 (17) |
| $\mathrm{C}(14)-\mathrm{O}(5) \quad 1$. | 1.458 (15) | $\mathrm{C}(14)-\mathrm{O}(6) \quad 1$ | 1.440 (17) |
| $\mathrm{C}(15)-\mathrm{C}(16) \quad 1$. | 1.307 (17) | $\mathrm{C}(15)-\mathrm{O}(6)$ 1. | $1 \cdot 376$ (17) |
| $\mathrm{C}(16)-\mathrm{C}(17) \quad 1$. | 1.534 (16) |  |  |
| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{C}(13)$ | $115 \cdot 8$ (11) | $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(3)$ | 122.2(11) |
| $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{O}(1)$ | 117.8 (11) | $\mathrm{C}(3)-\mathrm{C}(2)-\mathrm{O}(1)$ | 119.9 (10) |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ | 122.0 (10) | $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(11)$ | 118.1 (10) |
| $\mathrm{C}(4)-\mathrm{C}(3)-\mathrm{C}(11)$ | 119.8 (10) | $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{C}(5)$ | 116.3 (10) |
| $\mathrm{C}(3)-\mathrm{C}(4)-\mathrm{O}(2)$ | 122.8 (11) | $\mathrm{C}(5)-\mathrm{C}(4)-\mathrm{O}(2)$ | 120.9 (11) |
| $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{C}(6)$ | 122.7 (10) | $\mathrm{C}(4)-\mathrm{C}(5)-\mathrm{C}(10)$ | $120 \cdot 9$ (10) |
| $\mathrm{C}(6)-\mathrm{C}(5)-\mathrm{C}(10)$ | 116.3 (10) | $\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{C}(7)$ | 121.3 (10) |
| $\mathrm{C}(5)-\mathrm{C}(6)-\mathrm{O}(3)$ | 119.8 (10) | $\mathrm{C}(7)-\mathrm{C}(6)-\mathrm{O}(3)$ | 118.9 (10) |
| $\mathrm{C}(6)-\mathrm{C}(7)-\mathrm{C}(8)$ | 120.0 (11) | $\mathrm{C}(7)-\mathrm{C}(8)-\mathrm{C}(9)$ | 121.6 (10) |
| $\mathrm{C}(8)-\mathrm{C}(9)-\mathrm{C}(10)$ | 116.8 (10) | $\mathrm{C}(5)-\mathrm{C}(10)-\mathrm{C}(9)$ | 123.9 (10) |
| $\mathrm{C}(5)-\mathrm{C}(10)-\mathrm{O}(4)$ | $120 \cdot 2$ (10) | $\mathrm{C}(9)-\mathrm{C}(10)-\mathrm{O}(4)$ | $115 \cdot 8$ (10) |
| $\mathrm{C}(3)-\mathrm{C}(11)-\mathrm{C}(12)$ | 121.0 (10) | $\mathrm{C}(3)-\mathrm{C}(11)-\mathrm{O}(4)$ | 122.0 (9) |
| $\mathrm{C}(12)-\mathrm{C}(11)-\mathrm{O}(4)$ | 117.0 (9) | $\mathrm{C}(11)-\mathrm{C}(12)-\mathrm{C}(13)$ | ) $117.0(10)$ |
| $\mathrm{C}(11)-\mathrm{C}(12)-\mathrm{C}(17)$ | ) 132.3 (10) | $\mathrm{C}(13)-\mathrm{C}(12)-\mathrm{C}(17)$ | ) $110.7(9)$ |
| $\mathrm{C}(1)-\mathrm{C}(13)-\mathrm{C}(12)$ | 125.6 (11) | $\mathrm{C}(1)-\mathrm{C}(13)-\mathrm{O}(5)$ | 122.9 (10) |
| $\mathrm{C}(12)-\mathrm{C}(13)-\mathrm{O}(5)$ | 111.5 (9) | $\mathrm{C}(17)-\mathrm{C}(14) \mathrm{O}(5)$ | 106.6 (9) |
| $\mathrm{C}(17)-\mathrm{C}(14)-\mathrm{O}(6)$ | 105.4 (10) | $\mathrm{O}(5)-\mathrm{C}(14)-\mathrm{O}(6)$ | 107.7 (10) |
| $\mathrm{C}(16)-\mathrm{C}(15)-\mathrm{O}(6)$ | 115.2 (11) | $\mathrm{C}(15)-\mathrm{C}(16)-\mathrm{C}(17)$ | ) $108.6(10)$ |
| $\mathrm{C}(12)-\mathrm{C}(17)-\mathrm{C}(14)$ | ) $100 \cdot 2$ (9) | $\mathrm{C}(12)-\mathrm{C}(17)-\mathrm{C}(16)$ | ) 113.4 (9) |
| $\mathrm{C}(14)-\mathrm{C}(17)-\mathrm{C}(16)$ | 16) 101.2 (9) | $\mathrm{C}(10)-\mathrm{O}(4)-\mathrm{C}(11)$ | $120 \cdot 5$ (8) |
| $\mathrm{C}(13)-\mathrm{O}(5)-\mathrm{C}(14)$ | 109.0 (9) | $\mathrm{C}(14)-\mathrm{O}(6)-\mathrm{C}(15)$ | 108.2 (10) |

Table 3. Least-squares planes and deviations ( $\AA$ ) of atoms from each plane

The e.s.d.'s of the deviations are $\sim 0.015 \AA$.
(a) Xanthone skeleton

| $0.100 X+0.995 Y+0.005 Z=1.982^{*}$ |  |  |  |
| :--- | ---: | :--- | ---: |
| $\mathrm{C}(1)$ | -0.06 | $\mathrm{C}(2)$ | -0.05 |
| $\mathrm{C}(3)$ | -0.03 | $\mathrm{C}(4)$ | 0.02 |
| $\mathrm{C}(5)$ | 0.04 | $\mathrm{C}(6)$ | 0.06 |
| $\mathrm{C}(7)$ | 0.01 | $\mathrm{C}(8)$ | -0.03 |
| $\mathrm{C}(9)$ | -0.06 | $\mathrm{C}(10)$ | -0.03 |
| $\mathrm{C}(11)$ | 0.01 | $\mathrm{C}(12)$ | 0.08 |
| $\mathrm{C}(13)$ | 0.06 | $\mathrm{O}(2)$ | 0.01 |
| $\mathrm{O}(4)$ | -0.02 | $\mathrm{O}(1) \dagger$ | -0.13 |
| $\mathrm{O}(3) \dagger$ | 0.08 | $\mathrm{C}(14) \dagger$ | 0.43 |
| $\mathrm{C}(17) \dagger$ | 0.14 | $\mathrm{O}(5) \dagger$ | 0.18 |

(b) Five-membered ring comprising $\mathrm{C}(12), \mathrm{C}(13), \mathrm{C}(14), \mathrm{C}(17)$, and $O(5)$

| $0.219 X+0.973 Y-0.073 Z=2.153^{*}$ |  |  |  |
| :--- | ---: | ---: | ---: |
| $C(12)$ | 0.05 | $C(13)$ | 0.02 |
| $C(14)$ | 0.08 | $C(17)$ | -0.09 |
| O(5) | -0.05 |  |  |

(c) Five-membered ring comprising $\mathrm{C}(14), \mathrm{C}(15), \mathrm{C}(16), \mathrm{C}(17)$, and $O(6)$

| $0.793 X-0.573 Y+0.206 Z=3.793^{*}$ |  |  |  |
| :--- | ---: | ---: | ---: |
| C(14) | 0.08 | $C(15)$ | 0.01 |
| $C(16)$ | 0.03 | $C(17)$ | -0.06 |
| $O(6)$ | -0.06 |  |  |

[^1]found in related molecules. The skeleton of the present molecule is slightly twisted along its longitudinal axis to take a propeller-like form, while the skeleton in the $p$ bromobenzoate ester of sterigmatocystin took a bent form (Fukuyama, Tsukihara, Katsube, Tanaka, Hamasaki \& Hatsuda, 1975). The conformation of the ring $\mathrm{C}(12)-\mathrm{C}(13)-\mathrm{O}(5)-\mathrm{C}(14)-\mathrm{C}(17)$ approximates
a half-chair with $\mathrm{C}(14)$ and $\mathrm{C}(17)$ displaced on opposite sides of the plane through $\mathrm{C}(12), \mathrm{C}(13)$, and $\mathrm{O}(5)$, while that of $\mathrm{C}(14)-\mathrm{C}(17)-\mathrm{C}(16)-\mathrm{C}(15)-\mathrm{O}(6)$ is an envelope with $\mathrm{C}(14)$ displaced from the plane through $\mathrm{C}(15), \mathrm{C}(16), \mathrm{C}(17)$, and $\mathrm{O}(6) . \mathrm{C}(12)-$ $\mathrm{C}(17)-\mathrm{C}(14)-\mathrm{O}(5)$ and $\mathrm{C}(16)-\mathrm{C}(17)-\mathrm{C}(14)-\mathrm{O}(6)$ torsion angles are 13.6 and $11.2^{\circ}$, respectively, each of which is the largest of the values in related molecules so far determined (Fukuyama, Ashida, Katsube \& Kakudo, 1979). The molecules related by screw symmetry are stacked with respect to each other along the $b$ axis at the xanthone moieties with a dihedral angle of about $11^{\circ}$. The intermolecular short contact ( 2.83 $\AA$ ) between $\mathrm{O}(3)$ and $\mathrm{O}(2)$ of an adjacent molecule seems to be a van der Waals contact.

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[^1]:    ${ }^{*} X, Y$, and $Z$ are defined as $a x+c z \cos \beta, b y$, and $c z \sin \beta$ respectively.
    $\dagger$ Not included in the least-squares calculations.

